Errata: Simulating Astrophysical Magnetic Fields with Smoothed Particle Magnetohydrodynamics

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A collection of mistakes and errors in my PhD thesis. At least the ones that I've spotted. If you come across others not listed, please contact me.

Chapter 2

- Equation 2.24 (induction equation) has the wrong sign on both RHS terms. The correct equation is given by 2.21.
- Equation 2.38 (dispersion relation for MHD waves) is missing a square on the first term inside the large square root brackets to the right. It should read:

$$\frac{\omega^2}{k^2} = \frac{1}{2} \left(c_{\rm s}^2 + v_{\rm A}^2 \right) \pm \frac{1}{2} \left(\left(c_{\rm s}^2 + v_{\rm A}^2 \right)^2 - 4 c_{\rm s}^2 v_{\rm A}^2 \frac{k_z^2}{k^2} \right)^{1/2}$$

In this way, the maximum of the fast magnetosonic speed then reduces to $(c_s^2 + v_A^2)^{1/2}$, as expected.

• Equation 2.83 (derivation of SPMHD equations of motion) has a spurious dot product in the third term, and should read accordingly:

$$\partial L_{a} = m_{a} \mathbf{v}_{a} \cdot \partial \mathbf{v}_{a} - \sum_{b} m_{b} \frac{P_{b}}{\Omega_{b} \rho_{b}^{2}} \sum_{c} m_{c} (\partial \mathbf{r}_{b} - \partial \mathbf{r}_{c}) \cdot \nabla_{b} W_{ab}(h_{b})$$

$$+ \sum_{b} m_{b} \frac{B_{b}^{2}}{2\mu_{0}\Omega_{b} \rho_{b}^{2}} \sum_{c} m_{c} (\partial \mathbf{r}_{b} - \partial \mathbf{r}_{c}) \cdot \nabla_{b} W_{ab}(h_{b})$$

$$- \sum_{b} m_{b} \frac{\mathbf{B}_{b} \cdot \mathbf{B}_{b}}{\mu_{0}\Omega_{b} \rho_{b}^{2}} \sum_{c} m_{c} (\partial \mathbf{r}_{b} - \partial \mathbf{r}_{c}) \cdot \nabla_{b} W_{ab}(h_{b})$$

$$- \sum_{b} m_{b} \frac{\mathbf{B}_{b}}{\mu_{0}\Omega_{b} \rho_{b}^{2}} \cdot \sum_{c} m_{c} (\partial \mathbf{r}_{b} - \partial \mathbf{r}_{c}) \mathbf{B}_{b} \cdot \nabla_{b} W_{ab}(h_{b})$$

The subsequent equation (Equation 2.84) is written correctly.

• Equation 2.97 (thermal conductivity) has the wrong sign, as direct second derivatives in the manner of Brookshaw (1985) have positive sign out front. It should read:

$$\frac{\mathrm{d}u_a}{\mathrm{d}t} = \sum_b \frac{m_b}{\overline{\rho}_{ab}} \alpha_u v^u_{\mathrm{sig}}(u_a - u_b) \mathbf{\hat{r}}_{ab} \cdot \nabla_a W_{ab}(h_a)$$