## **Production Systems**

AI CLASS NOTES #6, JOHN SHIEH, 2012

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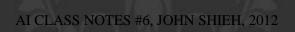
function depthsearch (current\_state);

#### % closed is global

#### begin

if current\_state is a goal
 then return SUCCESS;
add current\_state to closed;
while current\_state has unexamined children
 begin
 child := next unexamined child;
 if child not member of closed
 then if depthsearch(child) = SUCCESS
 then return SUCCESS
 end;
 return FAIL
end

% search exhausted



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function pattern\_search (current\_goal);

#### begin

if current\_goal is a member of closed then return FAIL else add current\_goal to closed; while there remain in data base unifying facts or rules do begin case current\_goal unifies with a fact: return SUCCESS; current goal is a conjunction  $(p \land ...)$ : begin for each conjunct do call pattern\_search on conjunct; if pattern\_search succeeds for all conjuncts then return SUCCESS else return FAIL end: current goal unifies with rule conclusion (p in  $q \rightarrow p$ ): begin apply goal unifying substitutions to premise (q); call pattern\_search on premise; if pattern\_search succeeds then return SUCCESS else return FAIL end; end; end: return FAIL end.

% test for loops

% end case

#### DEFINITION

#### PRODUCTION SYSTEM

A production system is defined by:

- The set of production rules. These are often simply called productions. A
  production is a condition-action pair and defines a single chunk of problemsolving knowledge. The condition part of the rule is a pattern that determines
  when that rule may be applied to a problem instance. The action part defines
  the associated problem-solving step.
- 2. Working memory contains a description of the current state of the world in a reasoning process. This description is a pattern that is matched against the condition part of a production to select appropriate problem-solving actions. When the condition element of a rule is matched by the contents of working memory, the action associated with that condition may then be performed. The actions of production rules are specifically designed to alter the contents of working memory.
- 3. The recognize-act cycle. The control structure for a production system is simple: working memory is initialized with the beginning problem description. The current state of the problem-solving is maintained as a set of patterns in working memory. These patterns are matched against the conditions of the production rules; this produces a subset of the production rules, called the conflict set, whose conditions match the patterns in working memory. The productions in the conflict set are said to be enabled. One of the productions in the conflict set is then selected (conflict resolution) and the production is

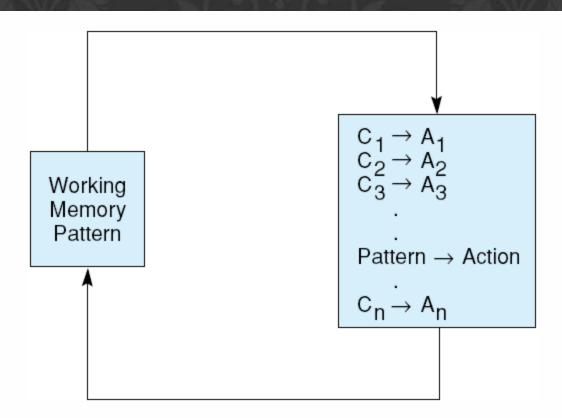
*fired.* To fire a rule, its *action* is performed, changing the contents of working memory. After the selected production rule is fired, the control cycle repeats with the modified working memory. The process terminates when the contents of working memory do not match any rule conditions.

*Conflict resolution* chooses a rule from the conflict set for firing. Conflict resolution strategies may be simple, such as selecting the first rule whose condition matches the state of the world, or may involve complex rule selection heuristics. This is an important way in which a production system allows the addition of heuristic control to a search algorithm.

The *pure* production system model has no mechanism for recovering from dead ends in the search; it simply continues until no more productions are enabled and halts. Many practical implementations of production systems allow backtracking to a previous state of working memory in such situations.

A schematic drawing of a production system is presented in Figure 6.1.

Fig 6.1 A production system. Control loops until working memory pattern no longer matches the conditions of any productions.



## Fig 6.2 Trace of a simple production system.

Production set:

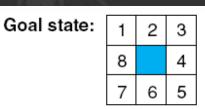
 $\begin{array}{rrrr} \mbox{1. ba} & \rightarrow & \mbox{ab} \\ \mbox{2. ca} & \rightarrow & \mbox{ac} \\ \mbox{3. cb} & \rightarrow & \mbox{bc} \end{array}$ 

Iteration #	Working memory	Conflict set	Rule fired
0	cbaca	1, 2, 3	1
1	cabca	2	2
2	acbca	2, 3	2
3	acbac	1, 3	1
4	acabc	2	2
5	aacbc	3	3
6	aabcc	Ø	Halt

### Fig 6.3 The 8-puzzle as a production system.

Start state:

2	8	З
1	6	4
7		5



#### Production set:

Condition

#### Action

goal state in working memory blank is not on the left edge blank is not on the top edge  $\rightarrow$  move the blank up blank is not on the right edge blank is not on the bottomedge  $\rightarrow$  move the blank down

 $\rightarrow$  halt

- $\rightarrow$  move the blank left
- $\rightarrow$  move the blank right

Working memory is the present board state and goal state.

#### Control regime:

- Try each production in order.
- 2. Do not allow loops.
- Stop when goal is found.

Fig 6.4 The 8-puzzle searched by a production system with loop detection and depth-bound, from Nilsson (1971).

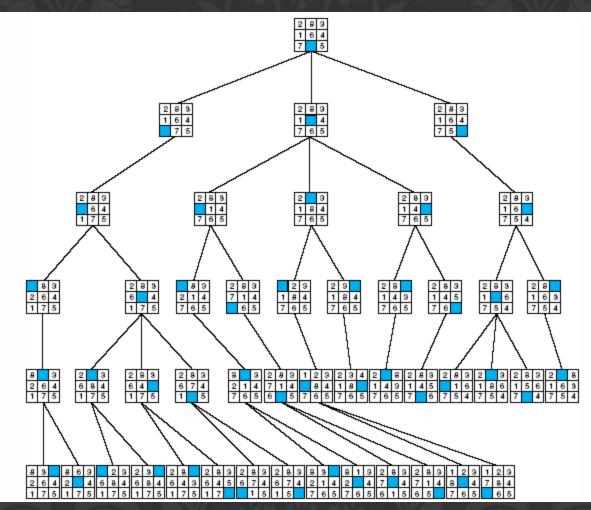
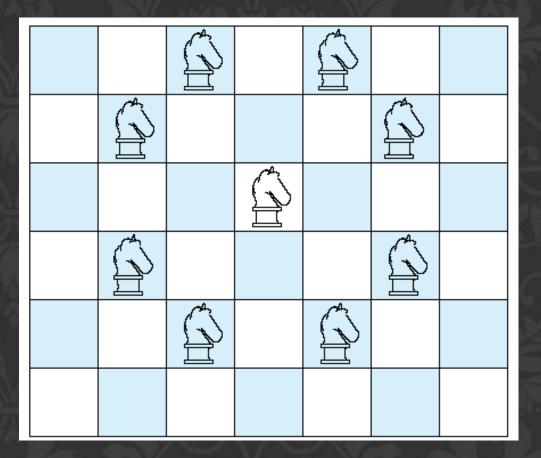


Fig 6.5 Legal moves of a chess knight.



# Fig 6.6 a 3 x 3 chessboard with move rules for the simplified knight tour problem.

1	2	3
4	5	6
7	8	9

move(1,8)	move(6,1)
move(1,6)	move(6,7)
move(2,9)	move(7,2)
move(2,7)	move(7,6)
move(3,4)	move(8,3)
move(3,8)	move(8,1)
move(4,9)	move(9,2)
move(4,3)	move(9,4)
1. 11. 1. 1. 1.	

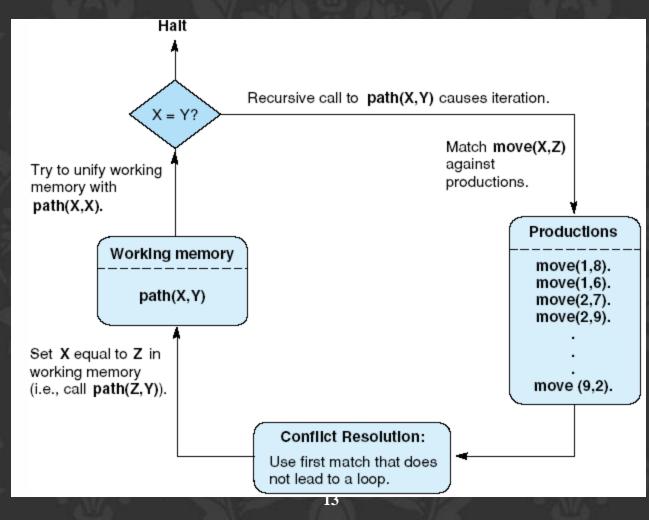
## Table 6.1 Production rules for the 3 x 3 knight problem.

RULE #	CONDITION		ACTION
1	knight on square 1	$\rightarrow$	move knight to square 8
2	knight on square 1	$\rightarrow$	move knight to square 6
3	knight on square 2	$\rightarrow$	move knight to square 9
4	knight on square 2	$\rightarrow$	move knight to square 7
5	knight on square 3	$\rightarrow$	move knight to square 4
6	knight on square 3	$\rightarrow$	move knight to square 8
7	knight on square 4	$\rightarrow$	move knight to square 9
8	knight on square 4	$\rightarrow$	move knight to square 3
9	knight on square 6	$\rightarrow$	move knight to square 1
10	knight on square 6	$\rightarrow$	move knight to square 7
11	knight on square 7	$\rightarrow$	move knight to square 2
12	knight on square 7	$\rightarrow$	move knight to square 6
13	knight on square 8	$\rightarrow$	move knight to square 3
14	knight on square 8	$\rightarrow$	move knight to square 1
15	knight on square 9	$\rightarrow$	move knight to square 2
16	knight on square 9	$\rightarrow$	move knight to square 4

## Fig6.7 A production system solution to the 3 x 3 knight's tour problem.

Iteration #	Working memory Current square Goal square		Conflict set (rule #'s)	Fire rule
0	1	2	1, 2	1
1	8	2	13, 14	13
2	3	2	5, 6	5
3	4	2	7, 8	7
4	9	2	15, 16	15
5	2	2		Halt

### Fig 6.8 The recursive path algorithm as production system.



#### Fig 6.9 Data-driven search in a production system.

Production set: 1.  $p \land q \rightarrow goal$ 

2.  $r \land s \rightarrow p$ 3.  $w \wedge r \rightarrow q$ 4. t  $\wedge u \rightarrow q$ 

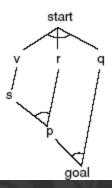
 $\rightarrow$  s 6. start  $\rightarrow v \land r \land q$ 

5. v

Trace of execution:

Iteration #	Working memory	Conflict set	Rule fired
0	start	6	6
1	start, v, r, q	6, 5	5
2	start, v, r, q, s	6, 5, 2	2
3	start, v, r, q, s, p	6, 5, 2, 1	1
4	start, v, r, q, s, p, goal	6, 5, 2, 1	halt

Space searched by execution:



Direction of search

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## Fig 6.10 Goal-driven search in a production system.

Production set: 1.  $p \land q \rightarrow goal$ 

 $\rightarrow$  s 6. start  $\rightarrow v \wedge r \wedge q$ 

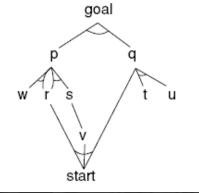
2.  $r \land s \rightarrow p$ 3.  $w \wedge r \rightarrow p$ 4.  $t \wedge u \rightarrow q$ 

5. v

Trace of execution:

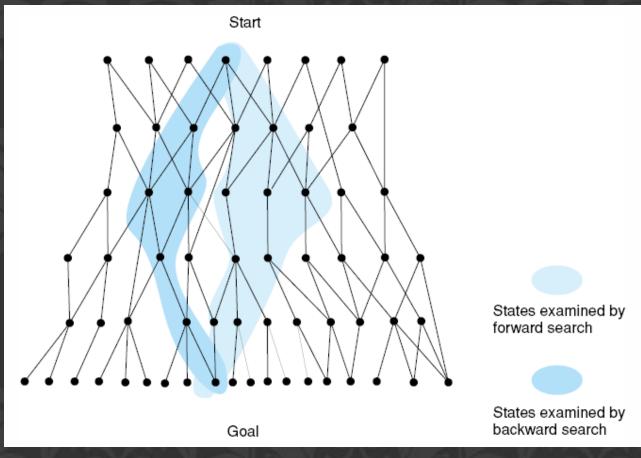
Iteration #	Working memory	Conflict set	Rule fired
0	goal	1	1
1	goal, p, q	1, 2, 3, 4	2
2	goal, p, q, r, s	1, 2, 3, 4, 5	3
3	goal, p, q, r, s, w	1, 2, 3, 4, 5	4
4	goal, p, q, r, s, w, t, u	1, 2, 3, 4, 5	5
5	goal, p, q, r, s, w, t, u, v	1, 2, 3, 4, 5, 6	6
6	goal, p, q, r, s, w, t, u, v, start	1, 2, 3, 4, 5, 6	halt

Space searched by execution:





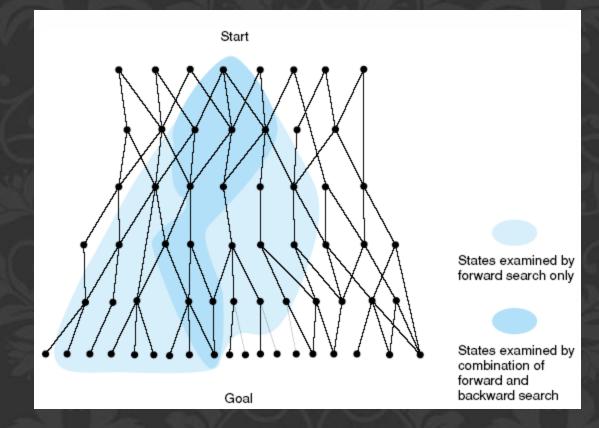
## Fig 6.11 Bidirectional search missing in both directions, resulting in excessive search.



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Fig 6.12 Bidirectional search meeting in the middle, eliminating much of the space examined by unidirectional search.



Major advantages of production systems for artificial intelligence

Separation of Knowledge and Control A Natural Mapping onto State Space Search Modularity of Production Rules Pattern-Directed Control Opportunities for Heuristic Control of Search Tracing and Explanation Language Independence A Plausible Model of Human Problem-Solving

## Fig 6.13 Blackboard architecture

