

Data Dependencies

(aka Procedural Dependency or Register Dependency)

Key factors for correctly running  $S_i$  and  $S_j$  (instructions) in parallel.

- ① They do not write into the same register.
- ② The input register(s) of one instruction do not overlap with the output of another instruction.

Berstein's Conditions of Detecting + Exploiting Data Dependencies (Data Parallelism)

- Consider two instructions ( $S_i$  and  $S_j$ )  
 $S_i: I_i \rightarrow O_i$  and  $S_j: I_j \rightarrow O_j$   
 where  $i < j$  ( $i$  is the "previous instruction" and  $j$  is the "subsequent instruction")

□ IO Dependency - Input [of the previous instruction] to Output [of the subsequent instruction]

$I_i \cap O_j = \{\emptyset\}$  iff  $S_i$  and  $S_j$   
do not have  
IO Dependency

2] OI dependency (Output [of the prev instruction] to Input [of the subsequent instruction] dependency)

$$O_i \cap I_j = \{\emptyset\} \text{ iff } S_i \text{ and } S_j \text{ do not have OI dependency}$$

3] OO dependency - (Output [of the prev inst] to Output [of the subsequent inst])

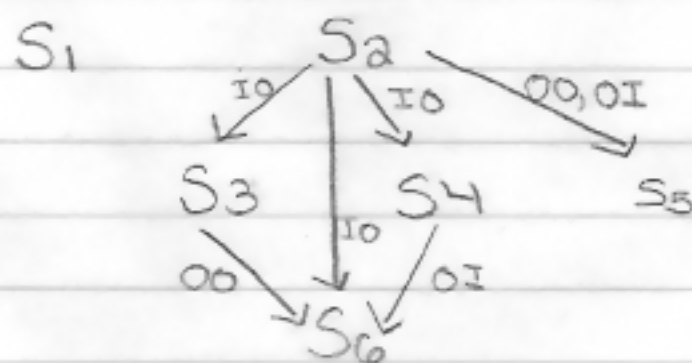
$$O_i \cap O_j = \{\emptyset\} \text{ iff } S_i \text{ and } S_j \text{ do not have OO dependency}$$

### Data Dependency Graph

Gives a directed graph showing data dependencies among pairs of instructions.

Example:

S <sub>1</sub> :	R <sub>6</sub> ←	R <sub>6</sub> *	R <sub>6</sub>	}	Program Segment "p"
S <sub>2</sub> :	R <sub>1</sub> ←	R <sub>2</sub> +	R <sub>3</sub>		
S <sub>3</sub> :	R <sub>2</sub> ←	R <sub>4</sub> *	R <sub>5</sub>		
S <sub>4</sub> :	R <sub>3</sub> ←	R <sub>3</sub> +	R <sub>4</sub>		
S <sub>5</sub> :	R <sub>1</sub> ←	R <sub>1</sub> +	R <sub>5</sub>		
S <sub>6</sub> :	R <sub>2</sub> ←	R <sub>3</sub> +	R <sub>4</sub>		

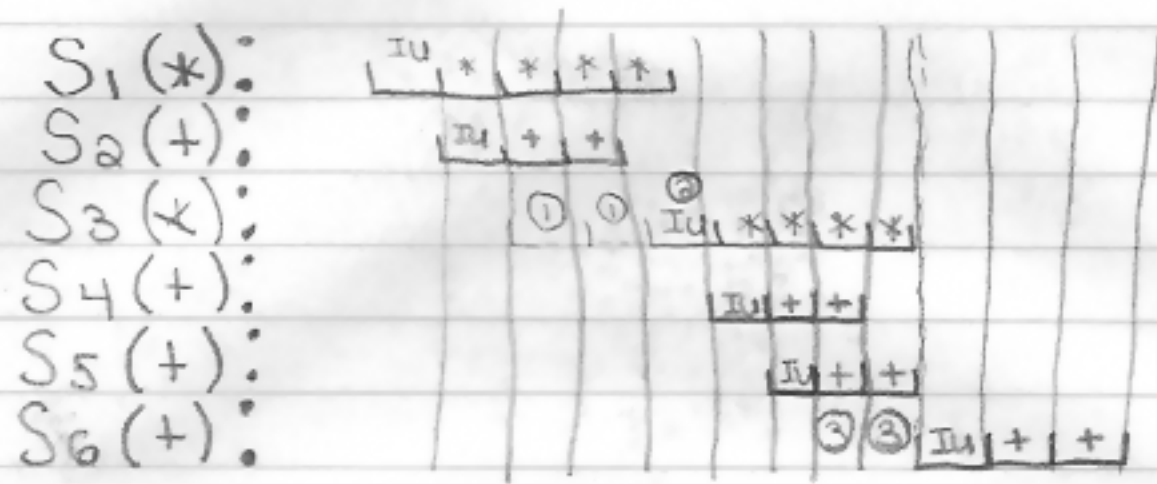


- ① The graph tells you about inherent parallelism (logical parallel) within a program.
- ② It allows for Instruction Rescheduling
- ③ Real Parallelism (no. of independent parallel units that the machine has)
- ④ Can also be done at the execution time
- ⑤ Use of the Transitive Closure Property for Simplifying Procedural Graphs
 

eg.  $S_a \rightarrow S_4 \rightarrow S_6$  covers  $S_a \rightarrow S_6$   
 Hence the edge  $S_a \rightarrow S_6$  can be removed w/o any loss of dependency information.
- ⑥ In a bigger context the graph is generated on a "chunk" of code at a time.

Ex: Given the last program segment (P) and machine  $M_1$ :

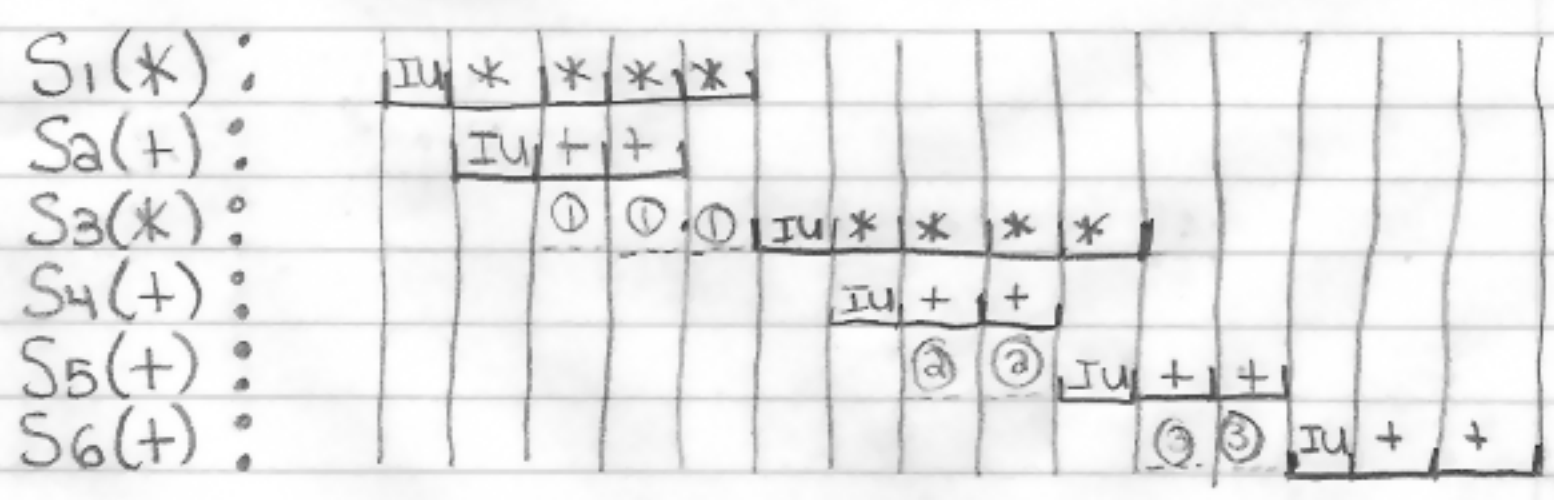
- infinite number of D units (ie. No D-unit conflict)
- + time: 2      \* time: 4
- IU time: 1



Annotations:

- ①  $S_3$  can not be issued at this time because  $S_3$  has a data dependency with  $S_2$ .
- ②  $S_3$  can be issued because it does not have dependency with  $S_1$ .
- ③  $S_6$  has a data dependency with  $S_3$ .

Ex2: Given the last program segment P and machine M:  
 - 1 adder, time = 2  
 - 1 multiplier, time = 4



Annotations:

- ①  $S_3$  has \* dependency with  $S_1$
- ②  $S_5$  has + dependency with  $S_4$
- ③  $S_6$  has + dependency with  $S_5$