



# COMP 4752

## Computational Intelligence

### **Lecture 23**

#### AI Programming Optimizations

# Bit Operations

- In low level languages like C, we can work directly with bit information in memory
- Bit operations are extremely fast, can be used to perform many initially unintuitive but useful functions
- Recall: An integer is a 32-bit value
- We can manipulate integers with bit ops

# Bit Operations

- Bitwise and &  
$$\begin{array}{r} 0101011101 \\ \& 1101010100 \\ = 0101010100 \end{array}$$
- Bitwise or |  
$$\begin{array}{r} 0101011101 \\ | 1101010100 \\ = 1101011101 \end{array}$$
- Bitwise xor ^  
$$\begin{array}{r} 0101011101 \\ \wedge 1101010100 \\ = 1000001001 \end{array}$$

# Bit Operations

- Bit LShift <<  
0001011100  
<< 3  
= 1011100000
- Bit RShift >>  
0001011100  
>> 3  
= 0000001011
- Bit Negation ~  
0101011101  
~= 1010100010

# Bit Sets

- One of the most common uses for working with bits is the concept of a **bit set**
- Bit sets are sets of bits of length  $N = 2^n$
- For example: 0101010110110010  $N = 16$
- Each element of the bit set typically represents a Boolean true or false, associated with the index in the set

# Bit Set Example

- We have a set of integers
  - $S = \{1, 4, 6, 7, 8, 12, 14\}$
- Can represent as a bit set of length  $N=16$ 
  - $B = 0100101110001010$
- We can store this in a 2-byte short in C
- We usually use a 4-byte int or 8-byte long
- ~No overhead going from short to int

# Bit Set Operations

- $\text{RONE} = 1 = 000\dots001$
- $\text{LONE} = 0x8000 = 100\dots000$
- Set containing single 1 in bit  $n$ 
  - $\text{RBIT}(n) : \text{RONE} \ll n$
  - $\text{LBIT}(n) : \text{LONE} \gg n$
- Test to see if set contains 1 in bit  $n$ 
  - $\text{TEST}(S, n) : S \ \& \ \text{BIT}(n)$

# Bit Set Operations

- Bit set intersection / union

- $S1 \ \& \ S2$   $S1 \ | \ S2$

- Add/remove set to/from set

- $S1 \ |= \ S2$   $S1 \ \&= \ \sim S2$

- Add/remove/toggle bit in a set

- $\text{ADDBIT}(S, \ n) :$   $S \ |= \ \text{BIT}(n)$

- $\text{REMOVEBIT}(S, \ n) :$   $S \ \&= \ \sim \text{BIT}(n)$

- $\text{TOGGLEBIT}(S, \ n) :$   $S \ \wedge= \ \text{BIT}(n)$

# Bit Set – Iterate Through Bits

```
S = 01010101010111
```

```
// iterate right to left
```

```
for (int b = RBIT(1); b != 0; b << 1)
    if (S & b)        // bit b is 1 in S
```

```
// iterate left to right
```

```
for (int b = LBIT(1); b != 0; b >> 1)
    if (S & b)        // bit b is 1 in S
```

# Bit Set Uses – Bit Boards!

- Many board games use 8x8 grids = 64
- One byte per position to store piece
- Bit boards can be used to store the positions of sets of pieces on the board
- In C, 64-bit long int can store board
- This will allow us to do many convenient AI related tasks in parallel

# Chess Bit Board

	a	b	c	d	e	f	g	h
1	0	1	2	3	4	5	6	7
2	8	9	10	11	12	13	14	15
3	16	17	18	19	20	21	22	23
4	24	25	26	27	28	29	30	31
5	32	33	34	35	36	37	38	39
6	40	41	42	43	44	45	46	47
7	48	49	50	51	52	53	54	55
8	56	57	58	59	60	61	62	63

	a	b	c	d	e	f	g	h
8	0	0	0	0	0	0	0	0
7	0	0	0	0	0	0	0	0
6	0	0	0	0	0	0	0	0
5	0	0	0	0	0	0	0	0
4	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	0
2	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0

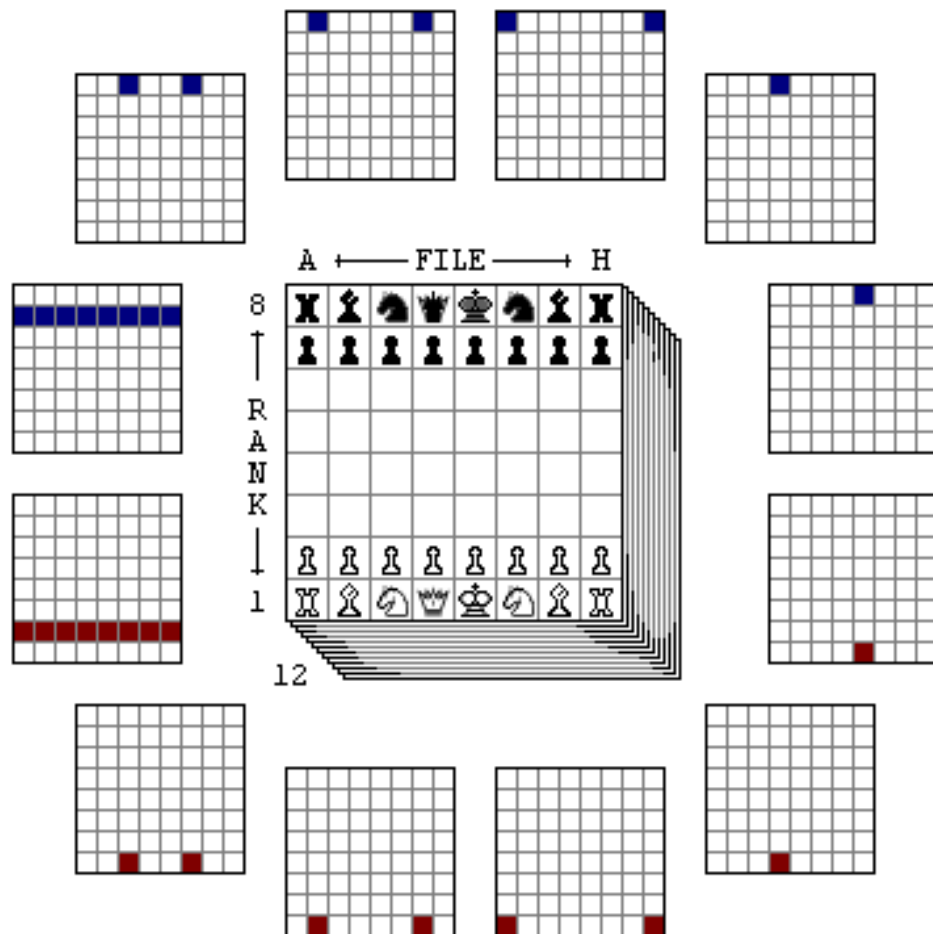
# Bit Board Representation

white pawns

A 7x7 grid of dots. Below each column of dots is the number 1, centered horizontally under the column.

# black rooks

A 10x10 grid of dots. The top-left dot (row 1, column 1) and the top-right dot (row 1, column 10) are labeled with the number '1'. All other dots in the grid are unlabeled.



# Bit Board - Union

white pieces		black pieces	=	occupied squares
. . . . .		1 . 1 1 1 1 1 1		1 . 1 1 1 1 1 1
. . . . .		1 1 1 1 . 1 1 1		1 1 1 1 . 1 1 1
. . . . .		. . 1 . . . .		. . 1 . . . .
. . . . .		. . . . 1 . . .		. . . . 1 . . .
. . . . 1 . . .		. . . . .	=	. . . . 1 . . .
. . . . . 1 . .		. . . . .		. . . . . 1 . .
1 1 1 1 . 1 1 1		. . . . .		1 1 1 1 . 1 1 1
1 1 1 1 1 1 . 1		. . . . .		1 1 1 1 1 1 . 1

# Bit Board - Intersection

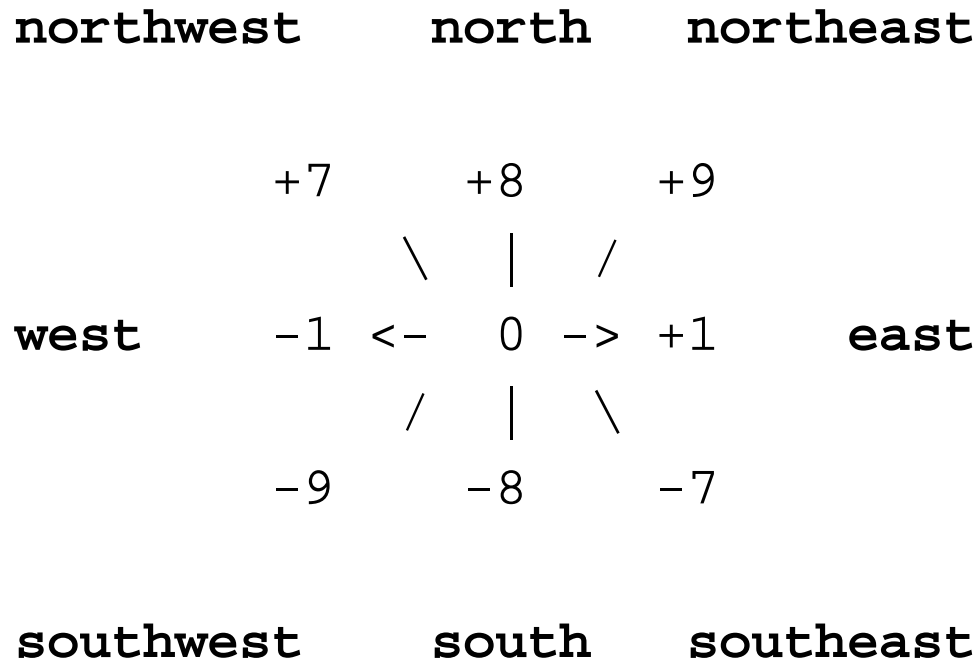
queen attacks      &      opponent pieces      =      attacked pieces

. . . . .	1 . . 1 1 . . 1	. . . . .
. . . 1 . . 1 .	1 . 1 1 1 1 1 .	. . . 1 . . 1 .
. 1 . 1 . 1 . .	. 1 . . . . . 1	. 1 . . . . .
. . 1 1 1 . . .	. . . . .	. . . . .
1 1 1 * 1 1 1 .	. . . * . . 1 .	. . . * . . 1 .
. . 1 1 1 . . .	. . . . .	. . . . .
. . . 1 . 1 . .	. . . . .	. . . . .
. . . 1 . . . .	. . . . .	. . . . .

# Bit Board - Negation

$$\begin{array}{rcccccccc}
 & \sim\text{occupied squares} & = & \text{empty squares} \\
 \\
 & 1 & . & 1 & 1 & 1 & 1 & 1 & 1 \\
 & 1 & 1 & 1 & 1 & . & 1 & 1 & 1 \\
 & . & . & 1 & . & . & . & . & . \\
 & . & . & . & . & 1 & . & . & . \\
 \sim & . & . & . & . & 1 & . & . & . \\
 & . & . & . & . & . & 1 & . & . \\
 & 1 & 1 & 1 & 1 & . & 1 & 1 & 1 \\
 & 1 & 1 & 1 & 1 & 1 & 1 & . & 1
 \end{array}
 =
 \begin{array}{rcccccccc}
 . & 1 & . & . & . & . & . & . \\
 . & . & . & . & 1 & . & . & . \\
 1 & 1 & . & 1 & 1 & 1 & 1 & 1 \\
 1 & 1 & 1 & 1 & . & 1 & 1 & 1 \\
 1 & 1 & 1 & 1 & . & 1 & 1 & 1 \\
 1 & 1 & 1 & 1 & 1 & . & 1 & 1 \\
 . & . & . & . & 1 & . & . & . \\
 . & . & . & . & . & . & 1 & .
 \end{array}$$

# Bit Boards – Direction Shift



# Bit Board – Population Count

- How many bits are 1 in a set?
  - MANY ways of doing this
  - MANY optimized versions
  - POPCOUNT hardware instructions
- 
- <https://chessprogramming.wikispaces.com/Population+Count>

# Bit Board Optimizations

- Many people have worked on chess specific optimizations for bit boards
- Functions for operations such as:
  - Is any piece attacking a given square
  - Is a given side attacking a given square
- These optimized functions are much faster than iterating over all cells

# Hashing Game Boards

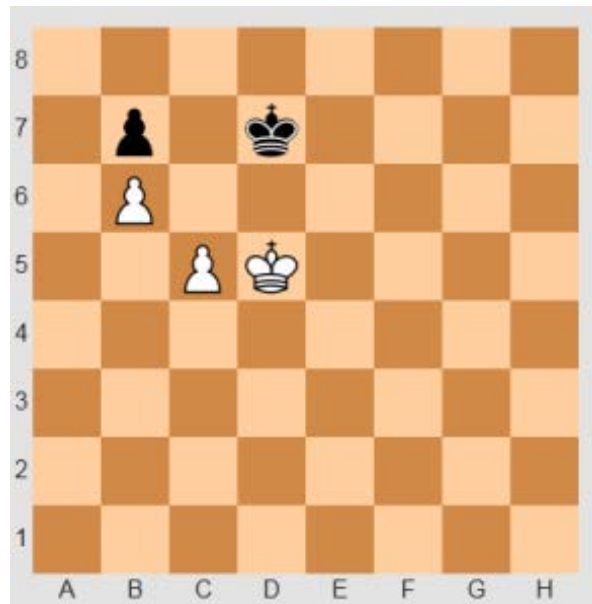
- Often we want to store information about a particular board configuration
- `Table[boardPosition] = ImportantInfo`
- We need a hash function which can turn a given board state into an integer
- One method: Zobrist Hashing

# Zobrist Hashing

- Zobrist relies makes use of two tools
  - Tables of random numbers
  - Bitwise XOR operator
- Create tables of random numbers representing pieces on given squares
  - `Z[Player][Piece][Square] = Random`
- Zobrist Hash Function
  - `Hash = XOR Z[Player][Piece][Square]` for all pieces

# Zobrist Hashing

- $Z[\text{White}][\text{Pawn}][\text{B6}] = R1$
- $Z[\text{White}][\text{Pawn}][\text{C5}] = R2$
- $Z[\text{White}][\text{King}][\text{D5}] = R3$
- $Z[\text{Black}][\text{Pawn}][\text{B7}] = R4$
- $Z[\text{Black}][\text{King}][\text{D7}] = R5$



- $\text{Zobrist Hash} = R1 \wedge R2 \wedge R3 \wedge R4 \wedge R5$

# Zobrist Hashing

- `Z[White][Pawn][B6]` = `R1`
- **`Z[White][Pawn][C5]` = **`R2`****
- `Z[White][King][D5]` = `R3`
- `Z[Black][Pawn][B7]` = `R4`
- `Z[Black][King][D7]` = `R5`



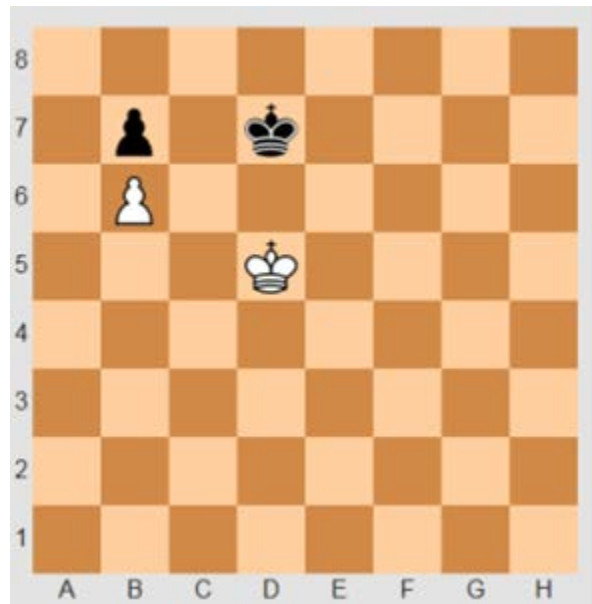
- `Zobrist Hash = R1 ^ R2 ^ R3 ^ R4 ^ R5`

# Zobrist Hashing

- Recall that XOR is reversible
- $A = 1001, B = 1101$
- $A \wedge B = 0100$
- $A \wedge B \wedge A = 1101 = B$
- $A \wedge A = 0000$
- We can remove a piece by applying XOR

# Zobrist Hashing

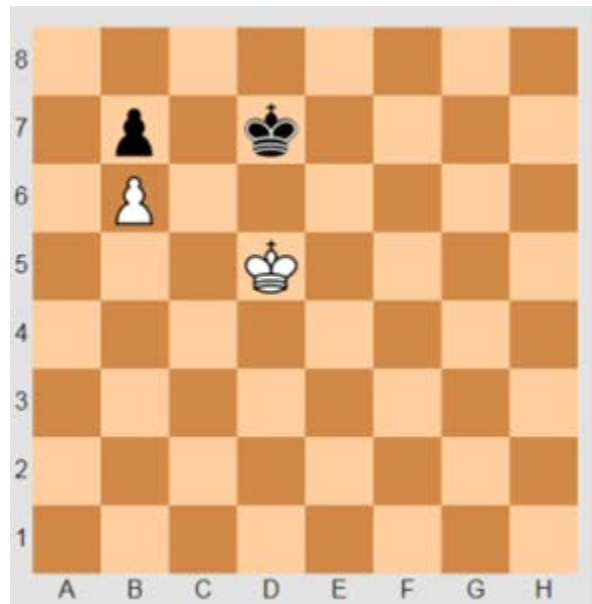
- `Z[White][Pawn][B6]` = `R1`
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- `Z[White][King][D5]` = `R3`
- `Z[Black][Pawn][B7]` = `R4`
- `Z[Black][King][D7]` = `R5`



- `Zobrist Hash = R1 ^ R2 ^ R3 ^ R4 ^ R5`

# Zobrist Hashing

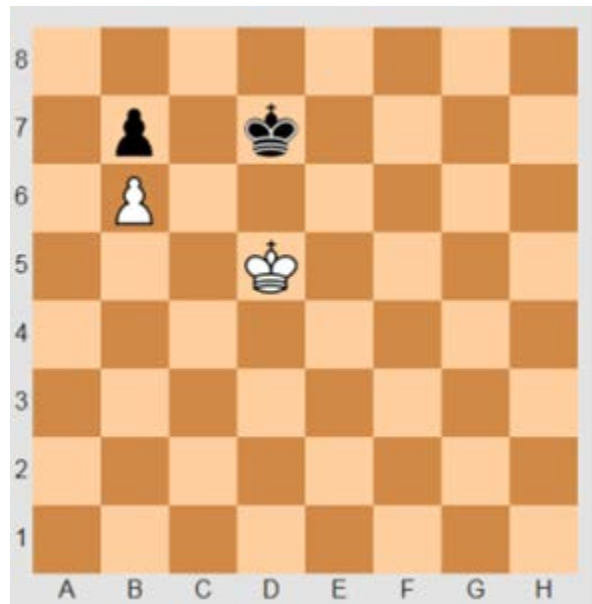
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- `Z[Black][Pawn][B7]` = `R4`
- `Z[Black][King][D7]` = `R5`



- `Zobrist Hash = R1 ^ R2 ^ R3 ^ R4 ^ R5 ^ R2`

# Zobrist Hashing

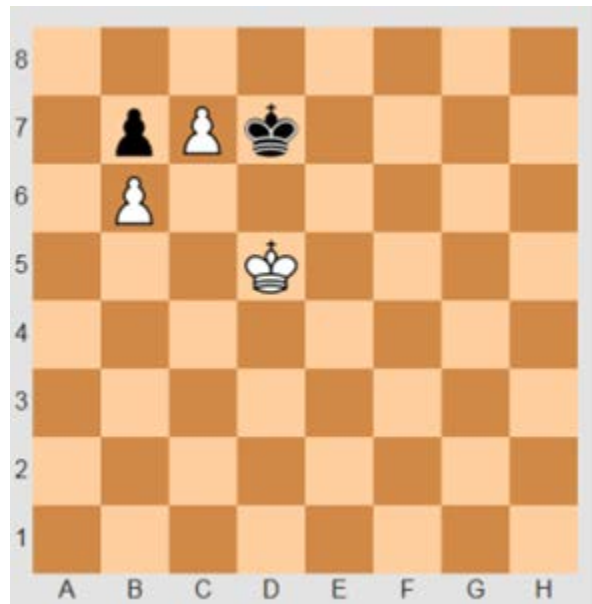
- $Z[\text{White}][\text{Pawn}][\text{B6}] = R1$
- $Z[\text{White}][\text{King}][\text{D5}] = R3$
- $Z[\text{Black}][\text{Pawn}][\text{B7}] = R4$
- $Z[\text{Black}][\text{King}][\text{D7}] = R5$



- $\text{Zobrist Hash} = R1 \wedge R3 \wedge R4 \wedge R5$

# Zobrist Hashing

- `Z[White][Pawn][B6]` = R1
- `Z[White][King][D5]` = R3
- `Z[Black][Pawn][B7]` = R4
- `Z[Black][King][D7]` = R5
- `Z[White][Pawn][C7]` = R6



- `Zobrist Hash = R1 ^ R3 ^ R4 ^ R5 ^ R6`

# Zobrist Hashing

- Zobrist Hashing is **incremental**
- When a piece is added, we simply XOR the existing hash by the Z-value
- When a piece is removed, we XOR the existing hash by the Z-value
- Moving a piece = remove then add at a different location = 2 XOR ops (3 if capt)