

LEWIS CARROLL Alice's Adventures in Wonderland and Through the Looking-Glass

COMP2000



Lecture 5 (last)



Logic: All, None, Some, and NOT



Admin stuff

- Quiz next Thursday, study guide to be posted by Monday.
- No lecture Tuesday: midterm break
- <u>Lab</u> questions?





 Susan is 28 years old, single, outspoken, and very bright. She majored in philosophy. As a student she was deeply concerned with issues of discrimination and social justice and also participated in anti-nuke demonstrations.

Please rank the following possibilities by how likely they are. List them from least likely to most likely.

- 1. a kindergarden teacher
- 2. works in a bookstore and takes yoga classes
- 3. an active feminist
- 4. a psychiatric social worker
- 5. a member of the Sierra club
- 6. a bank teller
- 7. an insurance salesperson
- 8. a bank teller and an active feminist



Universal Modus Ponens



- All men are mortal
- Socrates is a man
- Therefore, Socrates is mortal

- All cats like fish
- Molly likes fish



• Therefore, Molly is a cat



Universal Modus Ponens

- All men are mortal
- Socrates is a man
- Therefore, Socrates is mortal
- All numbers are either odd or even
- 2 is a number
- Therefore, 2 is either odd or even.
- All trees drop leaves
- Pine does not drop leaves
- Therefore, pine is not a tree



Negating the universal



- What is the opposite of "All"?
 - All girls hate math.
 - No!
 - All girls love math?
 - Some girls do not hate math!
 - Everybody in O'Brian family is tall
 - No, Jenny is O'Brian and she is quite short.
 - It is foggy all the time, every day in St. John's
 - No, sometimes it is not foggy (like today).

Negating the universal



- What is the opposite of "All"? \forall
- The negation of "All" is "Some" \exists
- "Some" may include all, but not necessarily.
- "Nobody" is not a negation of "All"
 - You wouldn't say "it is never foggy in St. John's" when somebody tells you it is always foggy. Sometimes it is, sometimes it isn't.
 - \forall x (if x is a number, then x is even or odd.)
 - $\exists x (x \text{ is a number and } x \text{ is prime})$
- Negation of \forall is \exists , and negation of \exists is \forall
 - Also, negation of -> is /\

Tricky universals



- Which statements are true?
 - All squares are white. All white shapes are squares
 - All circles are blue. All blue shapes are circles.



All lemurs live in the trees. All animals living in the trees are lemurs.

"NOT" makes life harder



- It is easy to visualize a tree, or a person
- It is harder to visualize a "not tree" or "not person"
- So "NOT (ALL trees have leaves)" is harder to understand than "some trees have something other than leaves (e.g., needles).
- Multiple negatives make it even harder
 - I vote against repealing the ban on smoking in public.
 - Do I like smoking in public?

Mixing quantifiers

- We can make statements of predicate logic mixing existential and universal quantifiers.
 - Predicate: X loves Y
 - Everybody loves somebody: $\forall X \exists Y (X \text{ loves } Y)$
 - Normal people
 - Somebody loves everybody: $\exists X \forall Y (X \text{ loves } Y)$
 - Mother Teresa
 - Everybody is loved by somebody $\forall X \exists Y$ (Y loves X)
 - Their mother
 - Somebody is loved by everybody $\exists X \forall Y$ (Y loves X)
 - Elvis Presley

Negating mixed quantifiers

- Now, a "not" in front of such a sentence means all ∀ and ∃ are interchanged, and the inner part becomes negated.
 - Predicate: X loves Y
 - Everybody loves somebody: $\forall X \exists Y (X \text{ loves } Y)$
 - Somebody does not love anybody $\exists X \forall Y NOT(X \text{ loves } Y)$
 - Somebody loves everybody: $\exists X \forall Y (X \text{ loves } Y)$
 - Everyone doesn't like somebody $\forall X \exists Y NOT(X \text{ loves } Y)$
 - Everybody is loved by somebody $\forall X \exists Y (Y \text{ loves } X)$
 - Somebody is not loved by anybody $\exists X \forall Y NOT(Y \text{ loves } X)$
 - Somebody is loved by everybody $\exists X \forall Y$ (Y loves X)
 - Everyone is not loved by somebody $\forall X \exists Y NOT(Y \text{ loves } X)$

Logic summary

- Propositional logic: A, B are either true or false
 - A and B: true if both are true
 - A or B: true if at least one is true
 - Not A: true if A is false
 - If A then B: true if either A is false, or both are true (equivalent to (not A or B).
- Predicate logic: Predicates are propositions with parameters: e.g., Odd(x) means number x is odd.
 - Universal quantifier: $\forall x \text{ Odd}(x) \text{all } x \text{ are odd}$.
 - Existential quantifier: $\exists x Odd(x) some x is odd$.

How do computers reason?

- They use logic (like one that we just studied)
 - For example, for relationships between concepts: if it is an animal, then it is alive.
- They use probabilities (which scenarios are more likely than other?)
- Fancy machine learning algorithms
- Example: IBM's "Watson" winning Jeopardy game.
- More to come...

