

Computer Science 3600 (Winter 2024):
 Assignment #1
 Supplementary Questions #2-6

2. (10 marks) For the algorithm below, derive a **worst-case** time complexity function $T(n)$.

```

i = 1
sum = 57
finished = false
while ((i <= n) and (not finished))
  for j = 1 to i do
    if (COND(i))
      sum = sum + (i/j)
      for k = 1 to log(n) do
        sum = sum + k
    else
      sum = sum - (j/i)
  if COND(sum) then
    finished = true
    i = 57
  else
    i = i + 1
sum = sum / i + 63

```

Note that method COND() runs in 4 timesteps.

3. (10 marks) For the algorithm below, derive an **asymptotic worst-case**, *i.e.*, Big-Oh, complexity function $O(f(n))$. Briefly explain the reasoning behind your derivation.

```

sum = 42
for i = 1 to n * log(n) do
  j = 1
  finished = false
  for k = 1 to n do
    if COND(sum)
      sum = sum / (k * i) + j
      while ((j <= n) and (not finished)) do
        finished = true

```

Note that method COND() runs in $(n + 13)$ timesteps.

4. (8 marks) For the algorithm below, derive a parameterized asymptotic worst-case time complexity function.

```

sum = 0
tsum = -15
for i = 1 to n do
  x = P1(n)
  sum = sum - x + 5
  for j = 1 to n * n do
    y = x / (P2(n) + P1(n))
    if (P3(n))
      if (P4(n))
        tsum = tsum + tsum
      else
        for j = 1 to log(n) do
          if (P4(n))
            y = y * i - j
          tsum = tsum / y
        sum = sum - tsum * tsum

```

5. (12 marks) Prove or disprove the following:

- a) (4 marks) $f(n) = (n - 2)(n - 6)$ is not $\Theta(n^2)$.
 - b) (4 marks) $f(n) = n^d + 10n^2$, where d is some integer constant greater than or equal to 2, is $O(n^d)$.
 - c) (4 marks) $f(n) = 10^{127}2^n$ is $\Omega(3^n)$.
6. (10 marks) Determine the longest common subsequence (LCS) of the strings GAAGCCTA and TATCGA using the algorithms given on pages 394 and 395 of the textbook. Show the filled-in dynamic programming matrix, all created matrix-cell backpointers (as arrows between matrix cells rather than in a separate matrix), the backpointer path that gives an optimal LCS, and the LCS associated with that path.